## UNIT-3 MPHYECC-5

## OP-AMP APPLICATIONS

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The electronic circuits, which perform arithmetic operations are known as arithmetic circuits. Using op-amps, we can build basic arithmetic circuits such as an adder and a subtractor. Here, you will learn about each of them in detail.

## Adder

An adder is an electronic circuit that produces an output, which is equal to the sum of the applied inputs. This section discusses about the op-amp based adder circuit.

An op-amp based adder produces an output equal to the sum of the input voltages applied at its inverting terminal. It is also called as a summing amplifier, since the output is an amplified one. The circuit diagram of an opamp based adder is shown in the following figure -


In the above circuit, the non-inverting input terminal of the op-amp is connected to ground. That means zero volts is applied at its non-inverting input terminal.

According to the virtual short concept, the voltage at the inverting input terminal of an op-amp is same as that of the voltage at its non-inverting input terminal. So, the voltage at the inverting input terminal of the op-amp will be zero volts.

The nodal equation at the inverting input terminal's node is

$$
\begin{gathered}
\frac{0-V_{i}}{R_{1}}+\frac{0-V_{2}}{R_{2}}+\frac{0-V_{0}}{R_{f}}=0 \\
=>\frac{V_{1}}{R_{1}}-\frac{V_{2}}{R_{2}}=\frac{V_{0}}{R_{f}} \\
V_{0}=R_{f}\left(\frac{V_{1}}{R_{1}}+\frac{V_{2}}{R_{2}}\right)
\end{gathered}
$$

If $\mathrm{R}_{\mathrm{f}}=\mathrm{R}_{1}=\mathrm{R}_{2}=\mathrm{R}$, then the output voltage $\mathrm{V}_{0}$ will be -

$$
\begin{gathered}
V_{0}=-R\left(\frac{V_{1}}{R}+\frac{V_{2}}{R}\right) \\
\Rightarrow V_{0}=-\left(V_{1}+V_{2}\right)
\end{gathered}
$$

Therefore, the op-amp based adder circuit discussed above will produce the sum of the two input voltages $V_{1}$ and $V_{2}$, as the output, when all the resistors present in the circuit are of same value. Note that the output voltage $\mathrm{V}_{0}$ of an adder circuit is having a negative sign, which indicates that there exists a $180^{\circ}$ phase difference between the input and the output.

## Subtractor

A subtractor is an electronic circuit that produces an output, which is equal to the difference of the applied inputs. This section discusses about the op-amp based subtractor circuit. An op-amp based subtractor produces an output equal to the difference of the input voltages applied at its inverting and noninverting terminals. It is also called as a difference amplifier, since the output is an amplified one.

The circuit diagram of an op-amp based subtractor is shown in the following figure -


Now, let us find the expression for output voltage $\mathrm{V}_{0}$ of the above circuit using superposition theorem using the following steps -

Step 1
Firstly, let us calculate the output voltage $\mathrm{V}_{01}$ by considering only $\mathrm{V}_{1}$. For this, eliminate $\mathrm{V}_{2}$ by making it short circuit. Then we obtain the modified circuit diagram as shown in the following figure -


Now, using the voltage division principle, calculate the voltage at the noninverting input terminal of the op-amp.

$$
=>V_{p}=V_{1}\left(\frac{R_{3}}{R_{2}+R_{3}}\right)
$$

Now, the above circuit looks like a non-inverting amplifier having input voltage $\mathrm{V}_{\mathrm{p}}$. Therefore, the output voltage $\mathrm{V}_{01}$ of above circuit will be

$$
V_{01}=V_{p}\left(1+\frac{R_{f}}{R_{1}}\right)
$$

Substitute, the value of $\mathrm{V}_{\mathrm{p}}$ in above equation, we obtain the output voltage $\mathrm{V}_{01}$ by considering only $\mathrm{V}_{1}$, as -

$$
V_{01}=V_{1}\left(\frac{R_{2}}{R_{2}+R_{3}}\right)\left(1+\frac{R_{f}}{R_{1}}\right)
$$

## Step 2

In this step, let us find the output voltage, $\mathrm{V}_{02}$ by considering only $\mathrm{V}_{2}$. Similar to that in the above step, eliminate $\mathrm{V}_{1}$ by making it short circuit. The modified circuit diagram is shown in the following figure.


You can observe that the voltage at the non-inverting input terminal of the op-amp will be zero volts. It means, the above circuit is simply an inverting op-amp. Therefore, the output voltage $\mathrm{V}_{02}$ of above circuit will be -

$$
V_{02}=-\left(\frac{R_{f}}{R_{1}}\right) \mathrm{V}_{2}
$$

## Step 3

In this step, we will obtain the output voltage $\mathrm{V}_{0}$ of the subtractor circuit by adding the output voltages obtained in Step1 and Step2. Mathematically, it can be written as

$$
\mathrm{V}_{0}=\mathrm{V}_{01}+\mathrm{V}_{02}
$$

Substituting the values of $\mathrm{V}_{01}$ and $\mathrm{V}_{02}$ in the above equation, we get -

$$
\begin{aligned}
& V_{0}=V_{1}\left(\frac{R_{3}}{R_{2}+R_{3}}\right)\left(1+\frac{R_{f}}{R_{1}}\right)+\left(-\frac{R_{f}}{R_{1}}\right) V_{2} \\
& =>V_{0}=V_{1}\left(\frac{R_{3}}{R_{2}+R_{3}}\right)\left(1+\frac{R_{f}}{R_{1}}\right)-\left(\frac{R_{f}}{R_{1}}\right) V_{2}
\end{aligned}
$$

If $R_{f}=R_{1}=R_{2}=R_{3}=R$, then the output voltage $V_{0}$ will be

$$
\begin{gathered}
=>V_{0}=V_{1}\left(\frac{R}{R+R}\right)\left(1+\frac{R}{R}\right)-\left(\frac{R}{R}\right) V_{2} \\
=>V_{0}=V_{1}\left(\frac{R}{2 R}\right)(2)-(1) V_{2} \\
\mathrm{~V}_{0}=\mathrm{V}_{1}-\mathrm{V}_{2}
\end{gathered}
$$

Thus, the op-amp based subtractor circuit discussed above will produce an output, which is the difference of two input voltages $V_{1}$ and $V_{2}$, when all the resistors present in the circuit are of same value.

